## Compound Curve

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A compound curve consist of 2 arcs of different radii bending in
the same direction and lying on the same side of their common
tangent. Then the center being on the same side of the curve.
$\mathrm{R}_{1}=$ Smaller radius
$\mathrm{R}_{2}=$ Larger radius
$\mathrm{T}_{\mathrm{S}}=$ smaller tangent length $=$ IT1
$\mathrm{Tl}=$ larger tangent length $=\mathrm{IT} 2$
$\Delta 1=$ deflection angle $\mathrm{b} / \mathrm{w}$ common tangent and rear tangent
$\Delta 2=$ angle of deflection $\mathrm{b} / \mathrm{w}$ common tangent and forward tangent
$\mathrm{D}=$ point of compound curvature MN
= common tangent


4 and $B I$ are two straights intersecting at $I$ (P.I.). $T_{1} D T_{2}$ is the compound curve pasisting of two arcs of radii $R_{1}$ and $R_{2}$ (Fig. 1 , and $D$ is the point of compound anature. $M N$ is the common tangent making deflection angles $\Delta_{1}$ and $\Delta_{2}$ at $M$ $\operatorname{dd} N$.
so that $\quad \Delta=\Delta_{1}+\Delta_{2}$
fom the triangle $I M N$,

$$
\frac{I M}{\sin \Delta_{2}}=\frac{I N}{\sin \Delta_{1}}=\frac{M N}{\sin \left(180^{\circ}-\left(\Delta_{1}+\Delta_{2}\right)\right)}
$$

Hence,

$$
I M=\frac{M N \sin \Delta_{2}}{\sin \left(\Delta_{1}+\Delta_{0}\right)}
$$

$$
I M=\frac{M N \sin \Delta_{2}}{\sin \Delta}
$$

Also,

$$
\begin{aligned}
& I N=\frac{M N \sin \Delta_{1}}{\sin \left(\Delta_{1}+\Delta_{2}\right)} \\
& I N=\frac{M N \sin \Delta_{1}}{\sin \Delta}
\end{aligned}
$$

## mon tangent MN

$$
\begin{aligned}
M D= & R_{1} \tan \frac{\Delta_{1}}{2} \\
D N= & R_{2} \tan \frac{\Delta_{2}}{2} \\
M N= & M D+D N \\
M N= & R_{1} \tan \frac{\Delta_{1}}{2} \\
& +R_{2} \tan \frac{\Delta_{2}}{2}
\end{aligned}
$$



Length of main tangents $\Pi_{1}$ and $\Pi_{2}$ :

$$
\begin{aligned}
\Pi_{1} & =T_{1} M+M I \\
& =R_{1} \tan \frac{\Delta_{1}}{2}+\frac{M N \sin \Delta_{2}}{\sin \Delta} \\
\Pi_{2} & =T_{2} N+N I \\
& =R_{2} \tan \frac{\Delta_{2}}{2}+\frac{M N \sin \Delta_{1}}{\sin \Delta}
\end{aligned}
$$

In total there are seven elements, viz. $\Delta_{1}, \Delta_{2}, \Delta, R_{1}, R_{2}, T_{2}$ and $\Pi_{1}$. If any fore of these elements are known (including at least one angle and at least two lenghs), be remaining three elements can be determined by applying the above equations.


A compound curve is normally set out by the method of deflection angles, using a theodolite (Fig $\quad 3$ The procedure for setting out a compound curve may be spit into office work and field work for the purpose of explanation.

## Office work

1. Calculate all the seven elements of the curve.
2. Locate P.I. (I), P.C. $\left(T_{1}\right)$ and P.T. $\left(T_{2}\right)$.
3. Calculate the chainage of $T_{1}$ (chainage of $I$ - tangent length $T_{2}$ )
4. Calculate the chainage of the point of compound curvature $D$.

$$
\text { Chainage of } D=\text { chainage of } T_{1}+\text { length of arc } T_{1} D
$$

$$
=\text { chainage of } T_{1}+\frac{\pi R_{1} \Delta_{1}}{180^{\circ}}
$$

5. Calculate the chainage of $T_{2}=$ chainage of $D+\pi R_{2} \Delta_{2} / 180^{\circ}$
6. Calculate the deflection angles for both the arcs from their tangents eg $\Delta_{1}=\delta_{1}=1718.9 C_{1} / R$, where $C_{1}$ is the chord length and $R$ is the radius

## Field work

## Fig 3

1. Set up the theodolite at $T_{1}$ and set out the first arc $T_{1} D$ by Rankine's method of deflection angles.
2. Shift the theodolite and set it up at point $D$.
3. Set the vernier A to read $\left(360^{\circ}-\Delta_{1} / 2\right)$, take a backsight on $T_{1}$ and uras the telescopes. Swing the telescope by $\Delta_{1} / 2$ so that the telescope is directert along $D N$ and vernier $A$ reads zero.
4. Now lay out the second are $D T_{2}$ in the same manner till $T_{2}$ is reached.
5. Check the observation by measuring the ane to $\left(180^{\circ}-\left(\Delta_{1}+\Delta_{2}\right) / 2\right)$ or $\left(180^{\circ}-\Delta / 2\right)$.


Question:1
A compound curve , consisting of two simple circular curves of radii 350 m and 500 m , is to be laid out between two straights . The angles of intersection between the tangents and the two straights are $25^{\circ}$ and $55^{\circ}$.Calculate the various elements of the d compound curve


## Question-2

The centre line of a new railway line is to be set out along a valley. The first straight AI bears $75^{\circ}$, whilst the connecting straight IB bears $120^{\circ}$, Due to site condition it has been decided to join the straights compound curve.

The first curve of radius is commences at T1,Situated 300 m from I on straight AI, and deflects through an angle of $25^{\circ}$ before joining $2^{\text {nd }}$ curve. calculate the radius of the $2^{\text {nd }}$ curve and distance of tangent point $\mathrm{T}_{2}$ from I on the straight IB.

$$
\begin{aligned}
& \Delta=120^{\circ}-75^{\circ}=45^{\circ} \\
& \Delta_{1}=25^{\circ}
\end{aligned}
$$

Hence,

$$
\Delta_{2}=20^{\circ}
$$

Tangent length $=M D=T_{1} M=R_{1} \tan \Delta_{1} / 2=500 \times \tan 12^{\circ} 30^{\prime}=110.8 \mathrm{~m}$. In triangle $M I N \angle N I M=180^{\circ}-\Delta=180^{\circ}-45^{\circ}=135^{\circ}$

Length $T_{1} I-T_{1} M=300-110.8=189.2 \mathrm{~m}$
Now,

$$
\begin{aligned}
M N & =\frac{I M \sin N I M}{\sin \Delta_{2}}=\frac{189.2 \times \sin 135^{\circ}}{\sin 20^{\circ}}=391.2 \mathrm{~m} \\
I N & =\frac{I M \sin \Delta_{1}}{\sin \Delta_{2}}=\frac{189.2 \times \sin 25^{\circ}}{\sin 20^{\circ}}=233.8 \mathrm{~m} \\
T_{2} N & =N D=M N-M D=M N-T_{1} M=391.2-110.8=280.4 \mathrm{~m} \\
T_{2} N & =R_{2} \tan \Delta_{2} / 2 \\
280.4 & =R_{2} \tan 10^{\circ} \\
R_{2} & =1590 \mathrm{~m} \\
I T_{2} & =I N+N T_{2}=233.8+280.4=514.2 \mathrm{~m}
\end{aligned}
$$

or


## Fig-5

$$
\Rightarrow \quad R_{2}=1590 \mathrm{~m}
$$

## Question no:3

Two tangents AB and BC intersect at B , another line DE intersect AB and BC at D and E such that angle $\mathrm{ADE}=150^{\circ}$ and angle $\mathrm{DEC}=140^{\circ}$. The radius of curve is 200 m and that of $2^{\text {nd }}$ is 300 m . Chainage of $B$ is 950m.Calculate all data necessary for setting out the curve.
dainge of $s$ is 950 m the cane.


$$
\begin{aligned}
& A_{1}=180^{\circ}-150^{\circ}=30^{\circ} \\
& \Delta_{2}=180^{\circ}-140^{\circ}=40^{\circ} \quad A=A_{1}+R_{2}=70^{\circ} \\
& \text { Q T1D } D=D T_{2}=R_{s} \tan \angle_{1}=200 \times \tan 15^{\circ}=53.58 \mathrm{~m} .
\end{aligned}
$$

$$
\text { (1) } T_{3} E=E T_{2}=m \tan A_{2}=300 \times \tan 20^{\circ}=109.19
$$

(3) $D E=D T_{2}+T_{2} E=53.58+109.19=162.77 \mathrm{~m}$.
y For $B D E A$

$$
\begin{aligned}
& \frac{D B}{\sin 40^{\circ}}=\frac{B E}{\sin 30}=\frac{D E}{\sin 110^{\circ}} \\
& D B=D E \times \frac{\sin 40^{\circ}}{\sin 110^{\circ}}=162.77 \times \frac{\sin 40^{\circ}}{\sin 110^{\circ}}=111.34 \mathrm{~m} . \\
& B E=\frac{\sin 30}{\sin 110^{\circ}}=162.77 \times \frac{\sin 30^{\circ}}{\sin 110^{\circ}}=86.61 \mathrm{~m} .
\end{aligned}
$$

$$
\begin{aligned}
& B T_{1}=B D+D T=111.34+53.56=164.92 \\
& B T 3=B E+E T 3=86.61+10917=195.8 m
\end{aligned}
$$

(5) Chaiqe 2 $\pi=950-164.72=785 \cdot 06 \mathrm{~m}$
(6) chyt cenelem $=\frac{\pi \times 200 \times 30^{\circ}}{180^{\circ}}=101.12$
(D) Cloge of $72=985.48+101772=889.88 \mathrm{~m}$.
(8) Lon cune lo, Lh $=\frac{71 \times 300 \times 1,0^{\circ}}{180^{\circ}}=209.44 \mathrm{~m}$
(9) chaye $T_{3}=889.80+209.4 y=1099.24 m$.

Devlection anheifor short aince
Takay a fall chord of 20 m .
No. 7 Fall chord $=5 \times 20=100$
lensthot subdurd $=104.72-\mathrm{N}=4.72$
$\delta$ For full chord $=\frac{17189 \times 20}{200}=2^{\circ} 31^{\prime} 53^{\prime \prime}$
$\delta \mathrm{m} \quad$ sut hor $t=\frac{1+1894.72}{200}=0^{\circ} 40^{\prime} 34^{\prime \prime}$
Chere
Totar deflection conste $=\Delta / 2=\frac{30}{2}=15^{\circ}$
calcuatey arte $=5 \times 2^{0} 51^{\prime} 53^{2 r}+0^{\circ} 40^{\prime} 30^{\prime \prime}=14^{\circ} 59^{\prime \prime} 59^{\prime \prime}$
deflectin ore for low che taray chel lent 3 om .

$$
=15^{\circ} \mathrm{sog}
$$

No of Full chor $1=30 \times 6=180^{\circ}$
lemh 7 subamd $=209 \cdot 44-180=29.44$
For falchrot $=\frac{17189 \times 30}{300}=2^{41} 51^{\prime} 53^{11}$
FF For Foncy subdm $=\frac{17189 \times 29}{300}=2^{\circ} 48^{\prime} 41^{\prime \prime}$

$$
\begin{aligned}
& \text { Tan deflectin gre }=M_{2}=\frac{40^{\circ}}{2}=20^{\circ}, 300 \\
& \text { calculatey ayse }=6 \times 2^{\circ} 51^{\prime} 33^{\prime \prime}+2^{\circ} 48^{\prime} 41^{\prime \prime}=19^{\circ} 59^{\prime} 59^{\prime \prime}
\end{aligned}
$$

## Compound Curves

Problem: Two tangents $A B$ \& $B C$ are intersected by a line $K M$. the angles AKM and KMC are $140^{\circ} \& 145^{\circ}$ respectively. The radius of $1^{\text {st }}$ arc is 600 m and of $2^{\text {nd }}$ arc is 400 m . Find the chainage of tangent points and the point of compound curvature given that the chainage of intersection point is 3415 m .

## Solution:

$$
\begin{aligned}
& \alpha=180^{\circ}-140^{\circ}=40^{\circ} \\
& \beta=180^{\circ}-145^{\circ}=35^{\circ} \\
& \emptyset=\alpha+\beta=75^{\circ} \\
& \mathrm{I}=180^{\circ}-75^{\circ}=105^{\circ} \\
& \mathrm{KT}_{1}=\mathrm{KN}=\mathrm{R}_{\mathrm{L}} \tan \left(\frac{\alpha}{2}\right)=600 \tan \left(40^{\circ} / 2\right) \\
& \mathrm{KT}_{1}=\mathrm{KN}=218.38 \mathrm{~m} \\
& \mathrm{MN}=\mathrm{MT}_{2}=\mathrm{R}_{\mathrm{S}} \tan \left(\frac{\beta}{2}\right)=400 \tan \left(35^{\circ} / 2\right) \\
& \mathrm{MN}=\mathrm{MT}_{2}=126.12 \mathrm{~m} \\
& \mathrm{KM}=\mathrm{MT}_{2}+\mathrm{MN}=218.38+126.12 \\
& \mathrm{KM}=344.50 \mathrm{~m}
\end{aligned}
$$



## Compound Curves

## Solution:

Fin $\triangle \mathrm{BKM}$, by sin rule

$$
\begin{aligned}
& \frac{B K}{\sin \beta}=\frac{M K}{\sin (I)} \\
& \mathrm{BK}=\frac{M K \sin \beta}{\sin (I)}=\frac{344.50 \times \sin 35^{\circ}}{\sin 105^{\circ}}=204.57 \mathrm{~m}
\end{aligned}
$$

$$
\mathrm{BM}=\frac{M K \sin \alpha}{\sin (I)}=\frac{344.50 \times \sin 40^{\circ}}{\sin 105^{\circ}}=229.25 \mathrm{~m}
$$

$$
\mathrm{T}_{\mathrm{L}}=\mathrm{KT}_{1}+\mathrm{BK}=218.38+204.57=422.95 \mathrm{~m}
$$

$$
\mathrm{T}_{\mathrm{S}}=\mathrm{MT}_{2}+\mathrm{BM}=126.12+229.25=355.37 \mathrm{~m}
$$

$$
\mathrm{L}_{\mathrm{L}}=\frac{\pi R L \alpha}{180^{\circ}}=\frac{\pi \times 600 \times 40}{180^{\circ}}=418.88 \mathrm{~m}
$$



$$
\mathrm{L}_{\mathrm{S}}=\frac{\pi R_{s} \beta}{180^{\circ}}=\frac{\pi \times 400 \times 30}{180^{\circ}}=244.35 \mathrm{~m}
$$

## Compound Curves

Solution:

$$
\begin{aligned}
& =3415 \mathrm{~m} \\
& =-422.95 \mathrm{~m} \\
& =2992.05 \mathrm{~m} \\
& =+418.88 \mathrm{~m} \\
& =3410.93 \mathrm{~m} \\
& =+244.35 \mathrm{~m} \\
& =3655.25 \mathrm{~m}
\end{aligned}
$$



