From Table 13.2, the value of $\alpha$ for a circular footing may be used for the square footing in this problem.

$$
\begin{aligned}
\text { For }(\mathrm{H} / \mathrm{B}) & =6 / 2=3.0 \\
\alpha & =0.29 \text { approx. } \\
\therefore \mu & =\mathrm{A}+\alpha(1-\mathrm{A}) \\
& =0.5+0.29(1-0.5) \\
& =0.65 \\
\therefore \rho_{\mathrm{c}} & =0.65 \rho_{\text {oed }}=0.65 \times 63.0 \\
& =40.6 \mathrm{~mm}
\end{aligned}
$$

$$
\begin{aligned}
\text { total final settlement } & =\rho_{\mathrm{i}}+\rho_{\mathrm{c}} \\
& =57.4+40.6 \\
& =98 \mathrm{~mm}
\end{aligned}
$$

### 13.4 SETTLEMENT OF STRUCTURES ON SANDY SOILS

Because of the difficulty of obtaining undisturbed samples of sandy soil and carrying out laboratory tests to measure the soil compressibility, calculations of settlement of structures on sandy soil are usually based upon field tests. Some techniques are based upon penetration resistance readings of the soil. One commonly used measure of penetration resistance is the so called standard penetration resistance, N , which is obtained in a dynamic penetration test in which the penetrometer consists of a split barrel sampler. With this test the sampler is driven by means of a 63.5 kilogram mass falling a distance of 760 mm to the top of the drill rods, the number of blows required to drive the sampler a distance of 300 mm being recorded as the standard penetration resistance N .

Using this standard penetration resistance, Terzaghi and Peck (1948) prepared a design chart based on the assumption that the allowable maximum settlement of a footing was 25 mm . It is now appreciated that this design chart was too conservative and Peck, Hanson and Thornburn (1974) have prepared a more realistic design chart which is shown in Figure 13.7. The horizontal lines in the figure indicate the soil pressure corresponding to a settlement of 25 mm . The chart is based on the observed behaviour of footings located at depths of 3 to 5 metres below the ground surface. The N values governing the footing behaviour therefore corresponded to an effective overburden pressure of approx. 0.1 MPa . Some engineers apply a factor of 1.5 to the allowable soil pressures obtained from Fig. 13.7, arguing that this figure is still overconservative. In the design of proposed footings, if the overburden pressure differs greatly from 0.1 MPa the N values should be corrected before the correlation in Figure 13.7 is used.

Gibbs and Holtz (1957) in an extensive laboratory study showed the way in which the standard penetration resistance is influenced by overburden pressure (Fig. 13.8). Gibbs and Holtz suggested that N values could be corrected for the effects of oberburden pressure by means of this diagram. If the N value at a depth corresponding to an effective overburden pressure of 0.1 MPa is considered to be a standard, the correction factor, $\mathrm{C}_{\mathrm{N}}$, recommended by Peck, Hanson and Thornburn (1974) is given by:

$$
\begin{equation*}
\mathrm{C}_{\mathrm{N}}=0.77 \log _{10}\left(2 / \mathrm{p}^{\prime}\right) \tag{13.11}
\end{equation*}
$$

where $\mathrm{p}^{\prime}$ is the effective overburden pressure in MPa . The equation is valid for $\mathrm{p}^{\prime} \geq 25 \mathrm{kPa}$. Equation (13.11) with a modification for low overburden pressures, is illustrated graphically in Fig. 13.9 Peck, Hanson and Thornburn (1974) have suggested that correction factors within the range 0.8 to 1.2 may be ignored without serious error.

The lines in Fig. 13.7 are drawn for the condition that the water table is at great depth. If the water table is located at a depth below the ground surface of less than ( $D+B$ ), Peck, Hanson and Thornburn (1974) have recommended that the soil pressures must be multiplied by a correction factor ( $\mathrm{C}_{\mathrm{w}}$ ) as follows:

$$
\begin{equation*}
\mathrm{C}_{\mathrm{w}}=0.5+0.5\left(\frac{\mathrm{D}_{\mathrm{w}}}{\mathrm{D}+\mathrm{B}}\right) \tag{13.12}
\end{equation*}
$$

where $D_{w}$ is the depth to the water table
D is the depth to the underside of the footing
B is the footing width.

Another measure of penetration resistance which is widely used is that obtained from a cone penetration test. (AS1289 F13.1). In this test, the point resistance is measured as the conical point of the penetrometer is gradually pushed into the ground. Meyerhof (1956) has suggested that the relationship between the cone penetration resistance $\left(\mathrm{q}_{\mathrm{c}}\right)$ and the standard penetration resistance N is given by the following expression

$$
\begin{equation*}
\mathrm{q}_{\mathrm{c}} \quad=\quad 400 \mathrm{~N} \mathrm{KPa} \tag{13.13}
\end{equation*}
$$

where $N$ is the uncorrected SPT value. In contrast Meigh and Nixon (1961) have shown that $\mathrm{q}_{\mathrm{c}}$ varies from 430 N to 1930 N kPa .


Fig 13.7 Design Chart for Proportioning Shallow Footing on Sand (after peck, hanson and thornburn, 1974)


Fig 13.8 Influence of Overburden Pressure on Penetration Resistance in Sands
(After Gibbs and Holtz, 1957)


Fig 13.9 Chart for Correction Of $\mathbf{N}$ - Values in sand for influence of Over-Burden Pressure (After Peck, Hanson and Thornburn, 1974)

If the Young's modulus of a sand deposit can be evaluated or estimated, settlement may be determined by means of the elastic displacement equation (13.4), the same one that was used for the calculation of immediate settlement. From the cone penetration resistance $\left(q_{c}\right)$ the Young's modulus ( $\mathrm{E}_{\mathrm{S}}$ ) of sandy soil may be determined by means of the following empirical expression

$$
\begin{equation*}
\mathrm{E}_{\mathrm{S}} \quad=\quad 2.5 \mathrm{q}_{\mathrm{c}} \tag{13.16}
\end{equation*}
$$

With this value of $\mathrm{E}_{\mathrm{S}}$ the settlement of a structure, supported on square footings on sand may also be determined by means of a semi-empirical procedure described by Schmertmann (1970, 1978).

Correlations have been developed between the compressibility $\left(\mathrm{m}_{\mathrm{v}}\right)$ and the cone penetration resistance $\left(\mathrm{q}_{\mathrm{c}}\right)$. Expressions relating the two are often of the form

$$
\begin{equation*}
\mathrm{m}_{\mathrm{v}} \quad=\quad 1 /\left(\alpha \mathrm{q}_{\mathrm{c}}\right) \tag{13.17}
\end{equation*}
$$

where $\alpha$ is a constant depending largely on the type of soil. This form of expression is widely used for clay soils. Tabulations of $\alpha$ values to be used with this expression have been given by Sanglerat (1972).


Fig 13.10 Definitions of Settlement

## EXAMPLE

The results of standard penetration tests in a medium-coarse sand are:

| HOLE NO. | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ |
| :---: | :---: | :---: | :---: | :---: |
| DEPTH (m) | Corrected N values |  |  |  |
| 1.0 | 3 | 5 | 4 | 7 |
| 2.0 | 15 | 12 | 13 | 20 |
| 3.0 | 14 | 18 | 14 | 22 |
| 4.0 | 21 | 24 | 18 | 18 |
| 5.0 | 27 | 22 | 20 | 31 |
| 6.0 | 30 | 34 | 38 | 36 |
| 10.0 | 52 | 47 | 60 | 42 |

(water table at 12 m )

Comment upon the proposal to place a 3 m by 4 m footing at a depth of 2.0 m to carry a load of 1.0 MN , if the settlement of the footing is to be limited to 25 mm .

For each hole the average N value over a depth below the proposed founding level equal to the footing width B should be determined. The average N values between depths of 2 m and 5 m are $19,19,16$ and 22 for holes $1,2,3$ and 4 respectively. The minimum N value of 16 is the one on which the assessment of the allowable soil pressure should be based.

From Fig. 13.7 for $\mathrm{B}=3 \mathrm{~m}, \mathrm{D} / \mathrm{B}=0.67$ and $\mathrm{N}=16$ allowable soil pressure $=0.16 \mathrm{MPa}$.
$\therefore$ load which can be safely carried by the footing

$$
\begin{array}{ll}
= & 0.16 \times 3 \times 4 \\
= & 1.92 \mathrm{MN}
\end{array}
$$

Since the allowable load exceeds the actual load, the footing settlement should not exceed 25 mm . Based upon settlement considerations the footing could be reduced in size.

### 13.5 ALLOWABLE SETTLEMENT

The stability and safety of a structure depends much more critically upon the distortion of the structure as a result of differential movements of the foundations than upon the absolute magnitude of the overall settlement of the foundation. Many buildings have experienced large settlements (even meters of settlement) without having undergone significant structural damage. In discussing allowable settlement of structures four measures of settlement are frequently used:
(a) $\quad \rho_{\max }$ the maximum settlement of any portion of the foundation
(b) $\quad \Delta \quad$ the maximum differential settlement between any two portions of the foundation
(c) $\quad(\delta / 1)$ the maximum angular distortion of buildings with columns, where $\delta$ is the differential settlement between the adjacent column footings and 1 is the column spacing
(d) relative deflection which is the ratio of the maximum settlement to the length of the structure.

Some of these definitions are illustrated in Fig. 13.10.

A number of observational studies have been carried out in an attempt to define the allowable settlement for buildings. From the results of a study of a large number of buildings, Skempton and MacDonald (1956) have recommended a range of maximum allowable settlements for structures. This information has been set out in Table 13.3. In this same table, Polshin and Tokar (1957) have quoted the recommended maximum average settlement values which are given in the Russian building code. The maximum settlements quoted in Table 13.3 are greater than the 25 mm value on which Fig. 13.7 is based. Although Fig. 13.7 may provide a conservative design, differential settlement rather than maximum settlement provides a more logical criterion for design as mentioned earlier.

TABLE 13.3

## MAXIMUM ALLOWABLE SETTLEMENTS FOR BUILDINGS AND LOAD BEARING WALLS

|  |  | Footings | Rafts |
| :--- | :--- | :---: | :---: |
| Maximum Settlement (mm) | Clays | 75 | 75 to 125 |
|  | Sands | 50 | 50 to 75 |
| Maximum Differential | Clays |  |  |
| Settlement (mm) | Sands |  | 45 |

(after Skempton \& MacDonald, 1956)

| Structure | Maximum Average <br> Settlement (mm) |
| :--- | :---: |
| Buildings with plain brick walls on continuous and separate <br> foundations (L = wall length, H = wall height) <br> L/H $\geq \quad 2.5$ <br> L/H $\leq \quad 1.5$ |  |
| Buildings with brick walls reinforced with reinforced <br> concrete or reinforced brick | 80 |
| Framed buildings | 100 |
| Solid reinforced concrete foundations of blast furnaces, <br> smoke stacks, silos, water towers, etc. | 150 |

(after Polshin \& Tokar, 1957)

The maximum settlement of a foundation is relatively easy to determine by means of one of the techniques previously discussed. The maximum differential settlement, however, is quite difficult to quantify. Fig. 13.11 has been prepared from a study of a large number of buildings located on both sandy and clayey soils. This diagram presents upper boundaries to the observed maximum differential settlements for particular values of observed maximum settlements. This figure indicates that in situations where the seat of settlement is located immediately beneath the foundation as in the case of sands the maximum differential settlement is almost identical with the maximum settlement. Smaller relative values of maximum differential settlement, however, are observed for structures founded on clay soils.

Observations of building settlements have indicated that the maximum angular distortion may be related in an approximate way to the maximum differential settlement as illustrated in Fig. 13.12. By making use of Figs. 13.11 and 13.12 a very rough idea of the maximum angular
distortion corresponding to a particular calculated value of the maximum settlement of a foundation may be obtained.

Regarding the maximum allowable values of angular distortion a number of recommendations have been made. Terzaghi (1935) from a study of the settlement of six buildings with load bearing brick walls concluded that the limiting angular distortion was in the vicinity of $1 / 280$. Skempton and McDonald (1956) have suggested that cracking of the panels in frame buildings is likely to occur if the angular distortion exceeds $1 / 300$. Other values of the angular distortion corresponding to a range of criteria are presented in Table 13.4. These figures apply to a sagging mode of distortion. Burland et al (1979) showed that if the deformation mode was hogging cracking occurred at much lower values of angular distortion.


Fig 13.11 Envelopes of Maximum Observed Differential Settlements
(After Bjerrum, 1962)


Fig 13.12 Observed relationship between Max. Differential Settlement and Max. Angular Distortion

TABLE 13.4
LIMITS OF ANGULAR DISTORTION OF BUILDINGS
(after Bjerrum, 1963)

| Criterion | Angular Distortion <br> $(\delta / 1)$ |
| :--- | :---: |
| Structural damage to building | $1 / 150$ |
| Safe limit for flexible brick walls $\left(\mathrm{H} / \mathrm{L}<\frac{1}{4}\right)$ | $1 / 150$ |
| Considerable cracking in panel walls and brick walls | $1 / 150$ |
| Difficulties with overhead cranes to be expected | $1 / 300$ |
| First cracking in panel walls to be expected | $1 / 300$ |
| Safe limit for buildings where cracking is not permissible | $1 / 500$ |
| Danger limit for frames with diagonals | $1 / 600$ |
| Limit where difficulties with machinery <br> settlements to be feared | $1 / 750$ |

Values of the recommended maximum allowable angular distortion taken from the Russian building code have been presented in Table 13.5.

TABLE 13.5

## MAXIMUM ALLOWABLE ANGULAR DISTORTION OF BUILDINGS AND LOAD BEARING WALLS <br> (after Polshin \& Tokar, 1957)

|  | Sand and Hard Clay | Plastic Clay |
| :---: | :---: | :---: |
| Angular distortion for: <br> (a) steel and reinforced concrete frame structures <br> (b) end rows of columns with brick cladding | $\begin{aligned} & .002 \\ & .007 \end{aligned}$ | $\begin{aligned} & .002 \\ & .001 \end{aligned}$ |
| Relative deflection of plain brick walls for: <br> (a) multi storey buildings $\begin{aligned} & \mathrm{L} / \mathrm{H} \leq 3 \\ & \mathrm{~L} / \mathrm{H} \geq 5 \\ & \mathrm{~L} \quad=\text { length of deflected part of wall, } \\ & \mathrm{H}=\text { wall height }) \end{aligned}$ <br> (b) one storey mills | $\begin{aligned} & .0003 \\ & .0005 \end{aligned}$ $001$ | . 0004 . 0007 $001$ |

### 13.6 BEARING CAPACITY OF STRIP FOOTINGS

The maximum bearing pressure that a foundation can support before the foundation soil fails is widely referred to as the ultimate bearing capacity. General shear failure of the foundation soil for a continuous or strip footing is considered to occur as shown in Fig. 13.13. The surface of sliding is along line KLM with a similar surface of sliding on the opposite side of the footing. A number of solutions for the ultimate bearing capacity ( $\mathrm{qult}_{\mathrm{ul}}$ ), in which various simplifying assumptions are made, have been developed. Prandtl (1921) has produced a solution for a surface footing $(\mathrm{D}=0)$ in which the foundation soil is assumed to be weightless. For this solution, which was carried out by means of the theory of plasticity, and angle $\psi$ is equal to $\left(45^{\circ}+\phi / 2\right)$.

With the Prandtl solution the underside HJ of the footing is smooth and three zones may be identified within the failure region. The zone indicated in Fig. 13.13 by the triangle JHK is an active Rankine zone, the zone indicated by the region KJL is a zone of radial shear with the line KL being a portion of a log spiral and the zone indicated by the triangle JLM is a passive Rankine zone.

If a surcharge pressure $q$ is considered to act on the surface of the ground, level with the underside of the foundation, an additional component is added to the ultimate bearing capacity. Reissner (1924) provided a solution for this surcharge component, which was also based on the theory of plasticity. These two bearing capacity components have been represented by means of the expression

$$
\begin{equation*}
\text { quit }=\mathrm{cN}_{\mathrm{c}}+\mathrm{qN}_{\mathrm{q}} \tag{13.18}
\end{equation*}
$$

where $\mathrm{N}_{\mathrm{c}}$ and $\mathrm{N}_{\mathrm{q}}$ are bearing capacity factors which are given by the following expressions:

$$
\begin{align*}
& \mathrm{N}_{\mathrm{q}}=\tan ^{2}\left(45^{\circ}+\phi / 2\right) \mathrm{e}^{\pi \tan \phi}  \tag{13.19}\\
& \mathrm{N}_{\mathrm{c}}==\left(\mathrm{N}_{\mathrm{q}}-1\right) \cot \phi \tag{13.20}
\end{align*}
$$

In the analyses by Prandtl and Reissner, it was assumed that the soil was weightless and the underside of the footing was perfectly smooth. In reality, however, soils possess weight and the underside of a footing is rarely smooth. These two aspects of the problem were taken into account in the solution presented by Terzaghi (1943). He assumed that the underside of the continuous footing was rough and the angle $\psi$ in Fig. 13.13 was equal to the angle of shearing resistance $\phi$. With the Terzaghi approach the wedge of soil JHK beneath the footing is treated as part of the footing. A surcharge or overburden pressure (q) will be present if the footing is located a distance below the ground surface. Terzaghi assumed that the soil above the foundation level HJM could be simply represented by the equivalent surcharge pressure q . The ultimate bearing capacity (qult) is determined


Fig 13.13 Assumed Mode of Failure for a Strip Footing


Fig 13.14 Terzaghi Bearing Capacity Factors for a Strip Footing
from considerations of vertical force equilibrium at the underside of the footing, and is usually made up of three components, a cohesion term, a surcharge term and a weight term, as follows

$$
\begin{equation*}
\mathrm{qult}=\mathrm{cN}_{\mathrm{c}}+\rho \mathrm{gDN}_{\mathrm{q}}+0.5 \rho \mathrm{~g} \mathrm{BN}_{\gamma} \tag{13.21}
\end{equation*}
$$

The dimensionless bearing capacity factors $\mathrm{N}_{\mathrm{c}}, \mathrm{N}_{\mathrm{q}}$ and $\mathrm{N}_{\gamma}$ are functions of the friction angle ( $\phi$ ), the Terzaghi values being given in Fig. 13.14. Several sets of bearing capacity factors are in current use in addition to the Terzaghi values. Vesic (1973) has identified many theoretical solutions for shallow foundations and a detailed discussion of some of these solutions has been presented by Bowles (1988).

Equation (13.21) may be used with either total or effective stresses. For short term bearing capacity calculations total stresses and undrained strength parameters, $c_{u}$ and $\phi_{u}$, should be used. For long term conditions effective stresses and drained strength parameters, $\mathrm{c}_{\mathrm{d}}$ and $\phi_{\mathrm{d}}$, should be used. The density $(\rho)$ in the surcharge term applies to the soil above foundation level, and the $\rho$ in the weight term applies to the soil below foundation level.

The greatest shortcoming of available theories lies in the assumption of incompressibility of the foundation soil. This means that the theories should be applied only to soils which are dense or stiff. Only in this way will the general failure pattern depicted in Fig. 13.13 and referred to as a general shear failure, develop. For softer or looser soils the footing tends to punch into the soil and the general failure pattern shown in that figure does not develop. There is no reliable theory which adequately takes into account the effect of soil compressibility in the calculation of bearing capacity. However, a footing on compressible soil may settle significantly under the effects of the footing loads and it is quite possible that settlement rather than shear failure may become the criterion for the design of the footing.

### 13.7 EFFECT OF FOOTING SHAPE AND DEPTH ON BEARING CAPACITY

Equation (13.21), which applies only to strip footings, has to be modified when circular, square or rectangular footings are used. This is usually done by multiplying the bearing capacity factors $\mathrm{N}_{\mathrm{c}}, \mathrm{N}_{\mathrm{q}}$ and $\mathrm{N}_{\gamma}$ by appropriate semi-empirical shape factors $\mathrm{s}_{\mathrm{c}}, \mathrm{s}_{\mathrm{q}}$ and $\mathrm{s}_{\gamma}$, respectively. There have been many suggestions regarding the magnitude of these shape factors. For example, Terzaghi and Peck (1967) have proposed the following expression for a circular footing of diameter B.

$$
\begin{equation*}
\text { quilt }=1.2 \mathrm{cN}_{\mathrm{c}}+\mathrm{ggDN}_{\mathrm{q}}+0.3 \rho \mathrm{~g} \mathrm{BN}_{\gamma} \tag{13.22}
\end{equation*}
$$

and the following for a square footing of width $B$

$$
\begin{equation*}
\mathrm{q}_{\text {ult }}=1.2 \mathrm{cN}_{\mathrm{c}}+\rho \mathrm{gDN}_{\mathrm{q}}+0.4 \rho \mathrm{~g} \mathrm{BN}_{\gamma} \tag{13.23}
\end{equation*}
$$

Shape factors for rectangular footings (B x L) according to Meyerhof (1963)

$$
\begin{equation*}
\mathrm{s}_{\mathrm{c}}=1+0.2 \mathrm{~K}_{\mathrm{p}}(\mathrm{~B} / \mathrm{L}) \tag{13.24}
\end{equation*}
$$

$$
\begin{align*}
& \mathrm{s}_{\mathrm{q}}=\mathrm{s}_{\gamma}=1+0.1 \mathrm{~K}_{\mathrm{p}}(\mathrm{~B} / \mathrm{L}) \text { for } \phi>10^{\circ}  \tag{13.25}\\
& \mathrm{s}_{\mathrm{q}}=\mathrm{s}_{\gamma}=1 \text { for } \phi=0 \tag{13.26}
\end{align*}
$$

where $K_{P}=\tan ^{2}\left(45+\frac{\phi}{2}\right)$

For a strip footing on a saturated clay soil the short term bearing capacity factors may be evaluated for the value of $\phi_{u}$ being equal to zero. For this condition the value of $\mathrm{N}_{\mathrm{q}}$ is equal to unity and the value of $\mathrm{N}_{\gamma}$ is zero. Equation (13.21) then simplifies to the following

$$
\begin{equation*}
\mathrm{q}_{\mathrm{ult}}=\mathrm{cN}_{\mathrm{c}}+\mathrm{q} \tag{13.27}
\end{equation*}
$$

For square or rectangular footings, Skempton (1951) has proposed the following expression for the bearing capacity factor $\mathrm{N}_{\mathrm{c}}$ for the case of $\phi=0$.

$$
\begin{equation*}
\mathrm{N}_{\mathrm{c}}(\text { rect })=\left(1+\frac{\mathrm{B}}{5 \mathrm{~L}}\right)\left(1+\frac{\mathrm{D}}{5 \mathrm{~B}}\right) \mathrm{N}_{\mathrm{c}} \text { (strip) } \tag{13.28}
\end{equation*}
$$

where $\quad B$ is the width of the footing
L is the length of the footing
D is the depth of the footing below the ground surface.

With this expression which contains both shape and depth factors, the maximum value of the ratio $\frac{D}{B}$ is 2.5 regardless of the actual value of $D$. Skempton has also proposed that with this expression the bearing capacity factor $\mathrm{N}_{\mathrm{c}}$ for a strip footing may be rounded from the Prandtl value of 13.14 to a value of 5 . The Skempton values of the bearing capacity factor $\mathrm{N}_{\mathrm{c}}$ for circular and square footings are shown in Fig. 13.15.

Various depth factors $\left(\mathrm{d}_{\mathrm{c}}, \mathrm{d}_{\mathrm{q}}, \mathrm{d}_{\gamma}\right)$ have been proposed and these are used as multipliers for the bearing capacity factors $\left(\mathrm{N}_{\mathrm{c}}, \mathrm{N}_{\mathrm{q}}, \mathrm{N}_{\gamma}\right)$ in a similar way to the shape factors. The Meyerhof (1963) values, for example, are

$$
\begin{equation*}
\mathrm{d}_{\mathrm{c}} \quad=\quad 1+0.2 \sqrt{K_{P}}(D / B) \tag{13.29}
\end{equation*}
$$



Fig 13.15 Short Term Bearing Capacity Factors for Foundations in Saturated Clay ( $\boldsymbol{\emptyset}_{\mathbf{u}}=\mathbf{0}$ )
(After Skempton, 1951)

$$
\begin{align*}
& \mathrm{d}_{\mathrm{q}}=\mathrm{d}_{\gamma}=1+0.1 \sqrt{\mathrm{~K}_{\mathrm{P}}}(\mathrm{D} / \mathrm{B}) \text { for } \phi>10^{\circ}  \tag{13.30}\\
& \mathrm{d}_{\mathrm{q}}=\mathrm{d}_{\gamma}=1 \text { for } \phi=0 \tag{13.31}
\end{align*}
$$

### 13.8 ALLOWABLE BEARING PRESSURE

For a strip footing (for purposes of discussion) the allowable bearing pressure ( $\mathrm{q}_{\text {all }}$ ), which is the pressure used to proportion the footing to support a given load, can be expressed in various ways
(a) as the quit (eq. (13.19)), often referred to as the gross ultimate bearing capacity, divided by an appropriate factor of safety (F) (Bowles, 1988),

$$
\begin{equation*}
\text { qall } \quad=\quad \mathrm{qult}^{\prime} / \mathrm{F} \tag{13.32}
\end{equation*}
$$

(b) as the net ultimate bearing capacity, which is defined as the gross ultimate bearing capacity less the overburden pressure at foundation level (q), divided by an appropriate factor of safety (Das, 1984),

$$
\begin{equation*}
q_{\text {all }}=\quad\left(q_{u l t}-q\right) / F \tag{13.33}
\end{equation*}
$$

(c) as in (b) but with the addition of the unfactored overburden pressure (Skempton, 1951),

$$
\begin{equation*}
q_{\text {all }}=\quad\left(q_{u l t}-q\right) / F+q \tag{13.34}
\end{equation*}
$$

On logical grounds equation (13.34) is the preferred one to use. In foundation design a value of 3 for F is widely used. For long term conditions where the analysis is carried out in terms of effective stress, Skempton (1951) gives the allowable bearing pressure as

$$
\begin{equation*}
\mathrm{q}_{\text {all }}=\frac{1}{\mathrm{~F}}\left(\mathrm{c}^{\prime} \mathrm{N}_{\mathrm{c}}+\mathrm{q}^{\prime}\left(\mathrm{N}_{\mathrm{q}}-1\right)+0.5 \mathrm{ggBN}_{\gamma}\right)+\mathrm{q} \tag{13.35}
\end{equation*}
$$

where $q^{\prime} \quad$ is the effective overburden pressure at foundation level
$\mathrm{q} \quad$ is the total overburden pressure at foundation level
and the bearing capacity factors are determined from the effective friction angle ( $\phi^{\prime}$ ).

If the foundation level is beneath the water table then the terms $q^{\prime}$ and $q$ will differ. The use of $q$ at the end of equation (13.35) allows for uplift for the submergence or partial submergence of the foundation. Also the density $(\rho)$ in the third term of the bearing capacity expression should be the buoyant density.

For short term conditions where the analysis is carried out in terms of total stresses, the allowable bearing pressure for a strip footing on a saturated cohesive soil may be written as

$$
\begin{equation*}
\mathrm{q}_{\text {all }}=\frac{\mathrm{c}_{\mathrm{u}} \mathrm{~N}_{\mathrm{c}}}{\mathrm{~F}}+\mathrm{q} \tag{13.36}
\end{equation*}
$$

## EXAMPLE

Determine the allowable bearing pressure that should be used for design of a square footing 3 m square. The footing is to be placed a distance of 2.5 m below the surface of a saturated clay soil. The water table is located a distance of 1.0 m below the ground surface.

Soil properties:

$$
\begin{array}{ll}
\text { saturated density } & =1.9 \mathrm{Mg} / \mathrm{m}^{3} \\
\text { undrained cohesion } & c_{\mathrm{u}}
\end{array}=110 \mathrm{kN} / \mathrm{m}^{2} .
$$

For determination of the allowable bearing pressure for short term conditions the undrained strength parameters should be used. A factor of safety of 3 will be used. If the Terzaghi \& Peck equation (13.23) is used, the ultimate bearing capacity is

$$
\begin{aligned}
\mathrm{q}_{\mathrm{ult}} & =1.2 \mathrm{c}_{\mathrm{u}} \mathrm{~N}_{\mathrm{c}}+\mathrm{qN}_{\mathrm{q}}+0.4 \rho \mathrm{gBN} \mathrm{~V}_{\gamma} \\
\text { for } \quad \phi_{\mathrm{u}} & =0^{\circ} \quad \text { from Fig. } 14.16 \\
\mathrm{~N}_{\gamma} & =0, \quad \mathrm{~N}_{\mathrm{q}}=1 \text { and } \mathrm{N}_{\mathrm{c}}=5.7 \\
\therefore \quad \mathrm{q}_{\mathrm{ult}} & =1.2 \mathrm{c}_{\mathrm{u}} \mathrm{~N}_{\mathrm{c}}+\mathrm{q} \\
\mathrm{q}_{\text {all }} & =\frac{1.2 \mathrm{c}_{\mathrm{u}} \mathrm{~N}_{\mathrm{c}}}{\mathrm{~F}}+\mathrm{q} \\
& =\frac{1.2 \times 110 \times 5.7}{3}+1.9 \times 10 \times 2.5 \\
& =251+48=299 \mathrm{kPa}
\end{aligned}
$$

If, alternatively, the value of $\mathrm{N}_{\mathrm{c}}$ was evaluated by means of the Skempton expression

$$
\begin{aligned}
\mathrm{N}_{\mathrm{c}} & =5\left(1+\frac{\mathrm{B}}{5 \mathrm{~L}}\right)\left(1+\frac{\mathrm{D}}{5 \mathrm{~B}}\right) \\
& =5(1+0.2)\left(1+\frac{2.5}{5 \times 3}\right) \\
& =7.0 \\
\therefore \quad \mathrm{q}_{\text {all }} & =\frac{\mathrm{c}_{\mathrm{u}} \mathrm{~N}_{\mathrm{c}}}{\mathrm{~F}}+\mathrm{q} \\
& =\frac{110 \times 7}{3}+48 \\
& =257+48=305 \mathrm{kPa}
\end{aligned}
$$

This value of allowable bearing pressure is only slightly different from the value calculated from equation (13.23). The short term allowable bearing pressure may be taken as approx. 300 kPa .

For long term conditions the calculation should be carried out in terms of effective stresses using the drained strength parameters. For $\phi_{d}=36^{\circ}$ from Fig. 13.14.

$$
\mathrm{N}_{\mathrm{c}}=63, \mathrm{~N}_{\mathrm{q}}=47, \mathrm{~N}_{\gamma}=51
$$

If the Meyerhof shape and depth factors are used

$$
\begin{array}{rlr}
\mathrm{K}_{\mathrm{P}}=\tan ^{2}\left(45+\frac{\phi}{2}\right) & =3.85 \\
\mathrm{~s}_{\mathrm{c}}=1+0.2 \times 3.85 \times 1 & =1.77 \\
\mathrm{~s}_{\mathrm{q}}=\mathrm{s}_{\gamma}=1+0.1 \times 3.85 \times 1 & =1.39 \\
\mathrm{~d}_{\mathrm{c}}=1+0.2 \times \sqrt{3.85} \times(2.5 / 3) & =1.33 \\
\mathrm{~d}_{\mathrm{q}}=\mathrm{d}_{\gamma}=1+0.1 \times \sqrt{3.85} \times(2.5 / 3) & =1.16
\end{array}
$$

The allowable bearing pressure is given by

$$
\begin{array}{ll}
\text { qall } & =\quad \frac{1}{\mathrm{~F}}\left(\mathrm{c}_{\mathrm{d}} \mathrm{~N}_{\mathrm{c}} \mathrm{~s}_{\mathrm{c}} \mathrm{~d}_{\mathrm{c}}+\mathrm{q}^{\prime}(\mathrm{Nq}-1) \mathrm{s}_{\mathrm{q}} \mathrm{~d}_{\mathrm{q}}+0.5 \rho_{\mathrm{b}} \mathrm{~B} \mathrm{BN}_{\gamma} \mathrm{s}_{\gamma} \mathrm{d}_{\gamma}\right)+\mathrm{q} \\
= & 1 / 3(15 \times 63 \times 1.77 \times 1.33+33(47-1) \times 1.39 \times 1.16 \\
& +0.5 \times 0.9 \times 10 \times 3 \times 51 \times 1.39 \times 1.16)+48 \\
= & 1 / 3(2225+2448+1110)+48 \\
= & 1976 \mathrm{kPa}
\end{array}
$$

Clearly the footing should be designed for the short term allowable bearing pressure of 300 kPa .


## FIGURE 13.16 COLLAPSE OF SOIL AFTER WETTING

### 13.9 COLLAPSIBLE SOILS

Metastable or collapsible soils are defined as any unsaturated soil that goes through a radical rearrangement of particles and decrease in volume upon wetting with or without additional loading. These soils are generally wind blown (aeolian) deposits in a loose state and often found in arid or semi-arid regions. Typical collapse behaviour is illustrated on the pressure - void ratio plot in Fig. 13.16. As discussed by Clemence and Finbarr (1981) the collapse susceptibility of a soil may be determined by means of the collapse potential (CP) which is defined as

$$
\begin{equation*}
C P \quad=\quad \Delta \mathrm{e}_{\mathrm{c}} /\left(1+\mathrm{e}_{\mathrm{o}}\right) \tag{13.36}
\end{equation*}
$$

where the symbols are given in Fig. 13.16. A guide to the severity of the problem is given in Table 13.6.

TABLE 13.6

$$
\begin{aligned}
& \text { COLLAPSE POTENTIAL VALUES } \\
& \text { (after Clemence \& Finbarr (1981)) }
\end{aligned}
$$

| CP <br> $\mathbf{( \% )}$ | Severity of Problem |
| :---: | :---: |
| $0-1$ | No problem |
| $1-5$ | Moderate trouble |
| $5-10$ | Trouble |
| $10-20$ | Severe trouble |
| 20 | Very severe trouble |

### 13.10 EXPANSIVE SOILS

These soils which undergo volume changes upon wetting and drying have been discussed in Chapter 2. Some considerations which may need to be explored in designing foundations on these soils include
(a) replacing or chemically stablizing the expansive soil beneath the foundation,
(b) control the amount of swelling or shrinking by the use of moisture barriers,
(c) design the foundations and the structures to withstand the ground movements,
(d) use deep foundations extending to a depth below the active zone of movement,
(e) load the soil to a pressure intensity to balance the swell pressure.

### 13.11 SANITARY LANDFILL

Some of the problems associated with building on sanitary landfill material have been discussed by Sowers (1968). The physical properties of the material are quite difficult to quantify and the use of plate load testing has been found to be very helpful (Moore and Pedler, 1977). Sanitary landfills have been found to undergo large continuous settlements over a long period of time. Some empirical expression for settlement rate have been developed by Yen and Scanlon (1975) based on studies of several landfill sites in California. A more detailed listing of methods of predicting settlement may be found in Oweis and Khera (1990).

### 13.12 PILE FOUNDATIONS

Pile foundations are commonly divided into two types, end or point bearing piles and friction piles depending upon whether the source of support is at the tip of the pile or is derived from skin friction around the perimeter of the pile. Piles may be used to transfer loads to a stronger stratum, to compact loose sands, to resist lateral forces, to provide foundations below scour level (eg. for a bridge crossing a river) or to provide an economic alternative to surface footings. Piles are commonly less than one meter in diameter and when their diameters are greater than this figure they are often referred to piers. Pile lengths are found to vary from 10 to 60 meters. The loads that piles are called upon to carry usually falls within the range of 200 kN to 2000 kN .

Many techniques having varying degrees of reliability may be used for the determination of the load carrying capacity of piles. Probably the most reliable technique is by means of a full scale pile load test in which a pile is loaded to failure in the field. This procedure is extremely expensive and would only be seriously considered for large projects. The results of pile load tests are not always conclusive since, as discussed by Chellis (1961) and Fellenius (1980), there are many ways in which the results of these tests may be interpreted.

A much less expensive and, for this reason, more popular method for determination of the ultimate load capacity of a pile $\left(\mathrm{Qult}_{\mathrm{ul}}\right)$, is by consideration of the end bearing and skin friction components separately.

$$
\begin{align*}
\mathrm{Q}_{\mathrm{ult}} & =\text { skin friction component }+ \text { end bearing component } \\
& =\pi \mathrm{BD} \mathrm{f}_{\mathrm{s}}+\mathrm{A}_{\mathrm{tip}} \cdot \mathrm{q}_{\mathrm{u}} \tag{13.37}
\end{align*}
$$

where the symbols are as given in Fig. 13.17. The skin friction $\left(f_{s}\right)$ is not necessarily constant and may vary considerably over the depth of the pile. In this case the skin friction component would need to be obtained by means of integration over the embedded length of the pile. The ultimate bearing capacity $\left(\mathrm{q}_{\mathrm{u}}\right)$ for the tip of the pile could be calculated by means of equation (13.22) assuming that the pile is circular is cross-section, and using $\mathrm{N}_{\mathrm{c}}, \mathrm{N}_{\mathrm{q}}$ and $\mathrm{N}_{\gamma}$ values appropriate for deep foundation (Fig 13.18).

For a cohesive soil the skin friction $\left(f_{s}\right)$ is equated to the adhesion $\left(\mathrm{c}_{\mathrm{a}}\right)$ and this is commonly related to the undrained cohesion ( $\mathrm{c}_{\mathrm{u}}$ ) by means of the expression

$$
\begin{equation*}
\mathrm{f}_{\mathrm{s}}=\quad \mathrm{c}_{\mathrm{a}}=\alpha \quad \mathrm{c}_{\mathrm{u}} \tag{13.38}
\end{equation*}
$$

where the adhesion factor $(\alpha)$ varies from unity for low $c_{u}$ values to around 0.3 when $c_{u}$ is equal to about 200kPa. More information is given in the SAA Piling Code (AS2159) and in Tomlinson
(1986). Building codes may also specify the allowable skin friction values which may be used for design.

With a uniform cohesive soil with a constant value of the skin friction over the length of the pile, the load in the pile is a maximum at the ground surface and decreases linearly with depth as illustrated in Fig. 13.17 (b). The load in the pile does not decrease linearly with depth in the case of a cohesionless soil as shown in part (c) of this figure. The reason for this is that the skin friction $\left(\mathrm{f}_{\mathrm{s}}\right)$ is not constant over the entire length of the pile but increases with increasing depth.

For a cohesionless soil the skin friction ( $\mathrm{f}_{\mathrm{s}}$ ) at any depth z below the ground surface may be expressed as follows

$$
\begin{align*}
\mathrm{f}_{\mathrm{s}} & =\sigma_{\mathrm{h}} \tan \delta \\
& =\mathrm{K} \sigma_{\mathrm{v}} \tan \delta \\
& =\mathrm{K} \rho \operatorname{gztan} \delta \tag{13.39}
\end{align*}
$$

where $\sigma_{h} \quad$ is the horizontal stress acting on the pile surface
$\sigma_{v} \quad$ is the vertical stress at a depth $z$ below the ground surface
$\delta \quad$ is the angle of friction for the pile surface
$\mathrm{K} \quad$ is an earth pressure co-efficient relating the horizontal to the vertical stress.


Fig 13.17 Load Distribution in Friction Piles

A number of proposals have been put forward regarding the evaluation of the parameters K and $\delta$ in equation (13.39). It has been suggested that the magnitude of the ( $\mathrm{K} \tan \delta$ ) varies from a value of 0.25 in loose sand to 1.0 in dense sand. Potyondy (1961) has shown that the angle $\delta$ may vary from approximately one-half of the angle of shearing resistance of the soil in the case of smooth steel piles in dry sand to a value equal to the angle of sharing resistance of the soil for a rough concrete pile in dry sand. Terzaghi and Peck (1967) have proposed a much simpler approach to the evaluation of skin friction and they have proposed values of $25 \mathrm{kN} / \mathrm{m}^{2}$ for long piles in loose sand and $100 \mathrm{kN} / \mathrm{m}^{2}$ for short piles in dense sand. For soil possessing both cohesional and frictional characteristics the skin friction may be evaluated by means of the following

$$
\begin{equation*}
\mathrm{f}_{\mathrm{s}} \quad=\quad \mathrm{c}_{\mathrm{a}}+\sigma_{\mathrm{h}} \tan \delta \tag{13.40}
\end{equation*}
$$

The load capacity of a pile may also be determined by means of a dynamic formula in which the ultimate supporting capacity of the pile is assumed to be equal to the ultimate driving resistance of the pile with an appropriate allowance for energy loss.

$$
\begin{equation*}
\mathrm{WH} \quad=\mathrm{RS}+\quad \text { energy loss } \tag{13.41}
\end{equation*}
$$

where the term WH is the energy input in which for a drop hammer, W would be the weight of the ram, H would be the height of fall. R is the driving resistance of the pile which is assumed to be equal to the ultimate load capacity of the pile and $S$ is the distance driven by the final blow.

Most dynamic formulas differ in the ways in which the energy loss is taken into account. The use of dynamic formulas for the calculation of the ultimate load capacity of a pile is not recommended for design although this procedure may be quite useful for construction control purposes.

For point bearing piles the skin friction component is commonly ignored although it is quite possible for a significant amount of the supporting capacity of the pile to be derived from this source. The total supporting capacity of a group of point bearing piles is often taken to be the sum of the individual supporting capacities of the piles making up the group. For a group of friction piles this is not found to be the case unless the pile spacing is very large in comparison with the pile diameter. For a group of friction piles driven into loose sand the group capacity is found to exceed the sum of the individual pile capacities due to the compacting effect of the pile driving on the sand. In the case of soft clay however, the group capacity is found to be less than the sum of the individual capacities.

This ratio of the group supporting capacity to the sum of the individual capacities of piles making up the group is referred to as the efficiency of the group. A number of efficiency
formulas have been proposed in an attempt to take this effect into account. Terzaghi and Peck (1967) have proposed that the ultimate supporting capacity of the pile group, $\mathrm{Q}_{\mathrm{g}}$, may be checked by assuming that the pile group behaves as one solid block or pier. They propose that the following expression should be used.

$$
\begin{equation*}
\mathrm{Q}_{\mathrm{g}} \quad=\quad \mathrm{qult} \mathrm{BL}+\mathrm{sD}(2 \mathrm{~B}+2 \mathrm{~L}) \tag{13.42}
\end{equation*}
$$

where B is the width of the pile group
L is the length of the pile group
s is the average shear strength of the soil over the embedded length $D$ of the pile group.

This type of block failure is very rarely associated with sandy soils but is much more commonly experienced with friction piles in clay soils.

Techniques for the determination of settlement of single piles and pile groups where the soil is assumed to be an elastic solid have been presented by Poulos (1968). For the calculation of settlements of pile groups in clay soils a rough procedure which is often used is one in which the group load is assumed to be concentrated either at the location of the pile tips or at a depth equal to two-thirds of the pile lengths.

A detailed presentation of pile foundation behaviour has been given by Poulos (1989).

## EXAMPLE

A group of nine timber piles $(3 \times 3)$ is driven 10 m into a saturated clay stratum. The pile diameter is 0.5 m and the pile spacing (centre to centre) in both directions is 1.0 m . The undrained cohesion of the clay is $60 \mathrm{kN} / \mathrm{m}^{2}$. Determine the ultimate load capacity of the pile group.

The capacity of a single pile is

$$
\begin{equation*}
\mathrm{Q}_{\mathrm{ult}} \quad=\pi \mathrm{BDf}_{\mathrm{s}}+\mathrm{A}_{\mathrm{tip}} \mathrm{qult} \tag{13.37}
\end{equation*}
$$

For $\quad c_{u} \quad=60 \mathrm{kPa}$, the SAA Piling Code suggests an $\alpha$ value of 0.8

$$
\therefore \quad \mathrm{f}_{\mathrm{s}} \quad=\mathrm{c}_{\mathrm{a}} \quad=\quad 0.8 \times 60=48 \mathrm{kPa}
$$

The net ultimate bearing capacity of the tip of the pile is

$$
\text { quit } \quad=\quad c_{u} N_{c}
$$

