

# FREQUENCY COMPENSATION

## INTRODUCTION

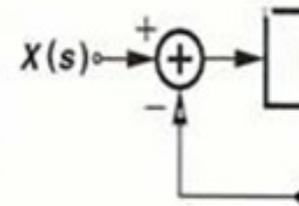
In this lecture, we deal with the stability and frequency compensation of linear feedback systems to the extent necessary to understand design issues of analog feedback circuits. Beginning with a review of stability criteria and the concept of phase margin, we study frequency compensation, introducing various techniques suited to different op amp topologies. We also analyze the impact of frequency compensation on the slew rate of two- stage op amps.



# BASIC NEGATIVE-FEEDBACK SYSTEM

- General considerations

- Close-loop transfer function:  $\frac{Y}{X}(s) = \frac{H(s)}{1 + \beta H(s)}$   
if  $\beta H(s = j\omega_1) = -1$ , the gain goes to infinity, and the circuit can amplify its own noise until it eventually begins to oscillate at frequency  $\omega_1$ .



- Barkhausen's Criteria:

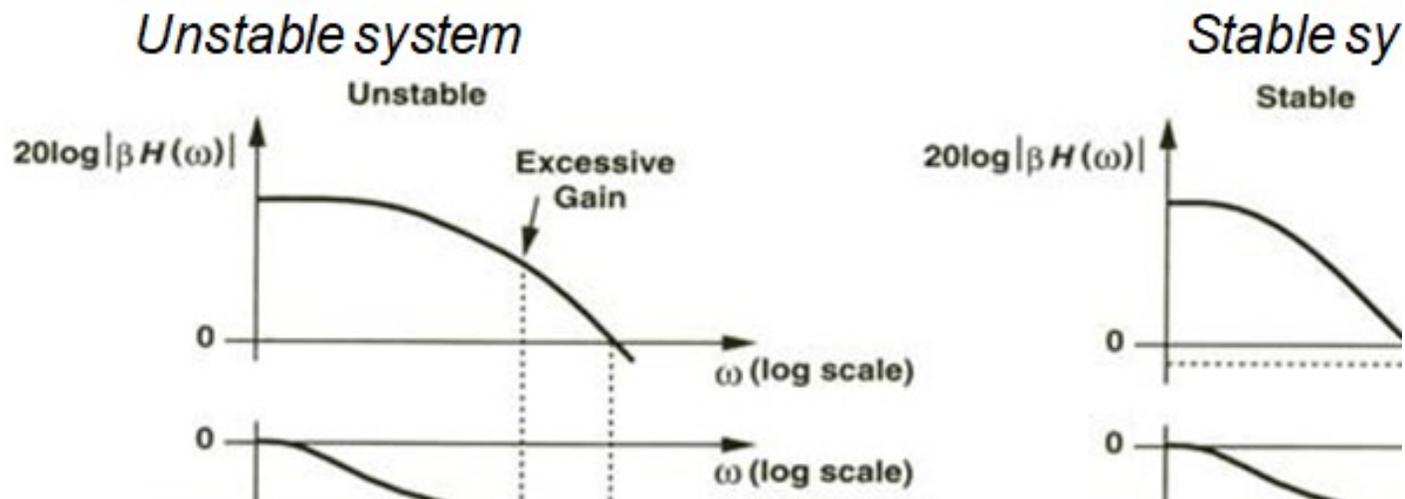
$$|\beta H(s = j\omega_1)| = 1$$

$$\angle \beta H(s = j\omega_1) = -180^\circ.$$

The total phase shift around the loop at  $\omega_1$  is  $360^\circ$  because feedback itself introduces  $180^\circ$  of phase shift. The  $360^\circ$  phase shift

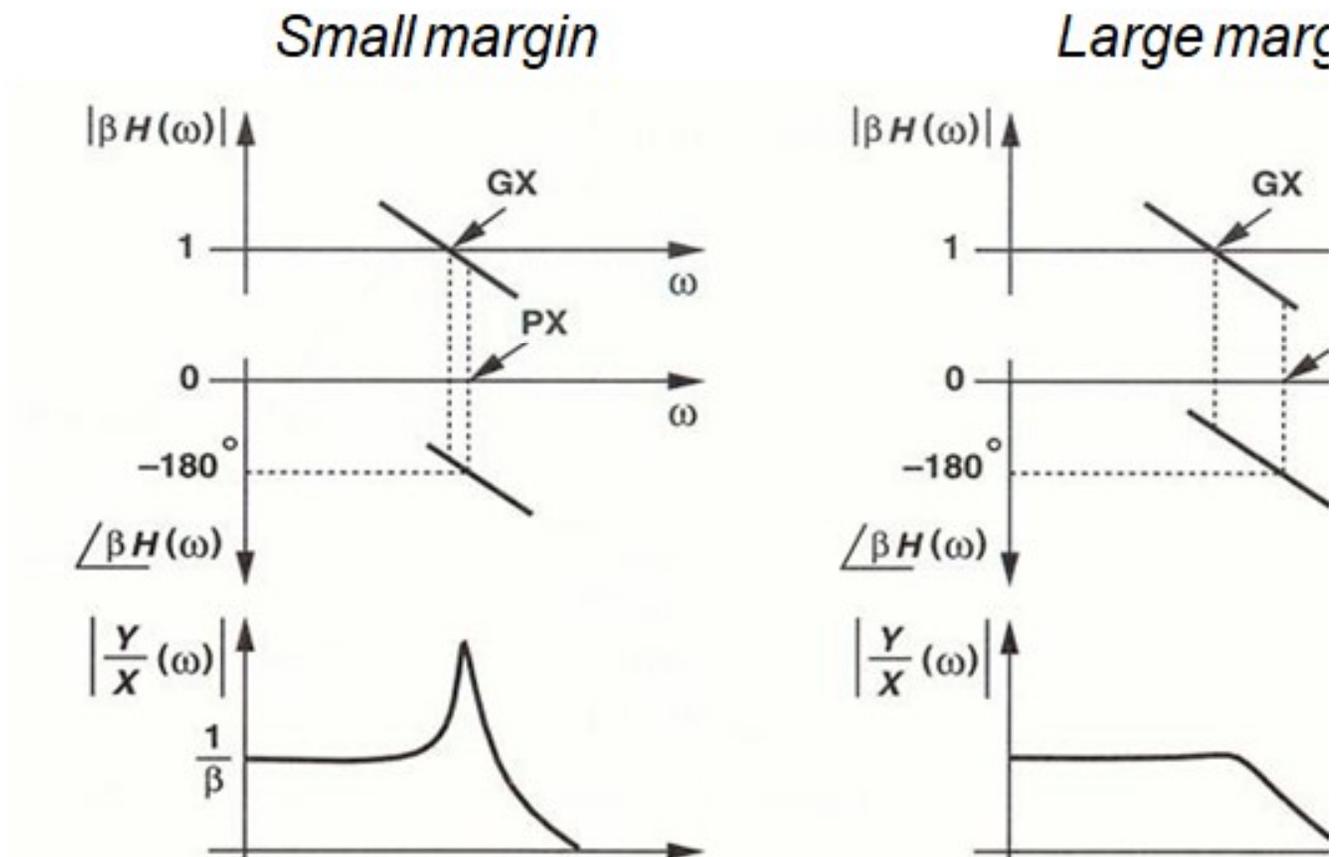
# BODE PLOT

- A negative feedback system may oscillate at  $\omega_1$  if
  - (1) the phase shift around the loop at this frequency is so much that the feedback becomes *positive*.
  - (2) the loop gain is still enough to allow signal buildup.



# Phase margin

- Close-loop frequency and time response



## Phase margin (cont'd)

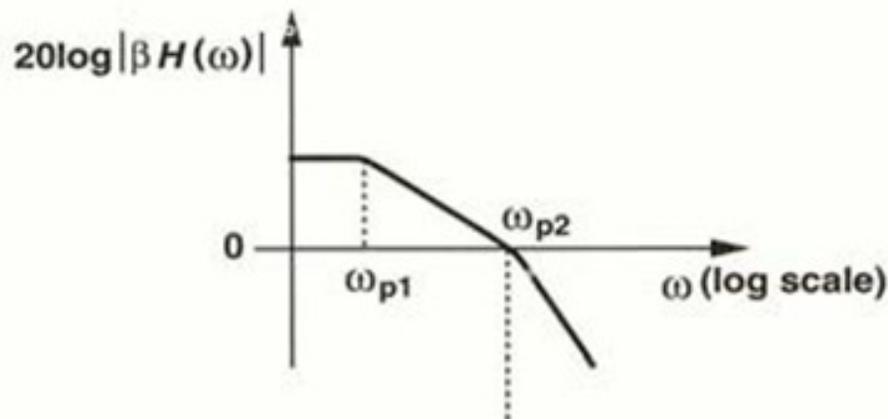
- *Phase margin* (PM) is defined as

$$PM = 180^\circ + \angle \beta H(\omega = \omega_1)$$

where  $\omega_1$  is the gain crossover frequency.

- Example

A two-pole feedback system is designed such that  $|\beta H(\omega = \omega_1)| = 1$  and  $|\omega_{P1}| \ll |\omega_{P2}|$ .



Since  $\angle \beta H$  reaches

## How much phase margin is adequate?

- For  $PM = 45^\circ$ , at the gain crossover frequency  $\angle \beta H(\omega_1) = -135^\circ$ ,  $|\beta H(\omega_1)| = 1$ , yielding  $\frac{Y}{X} = \frac{H(j\omega_1)}{1 + H(j\omega_1)} = \frac{-H(j\omega_1)}{1 + 1 \cdot \exp(-j135^\circ)} = \frac{0.29 - 0.71j}{0.29 - 0.71j}$

It follows that  $\left| \frac{Y}{X} \right| = \frac{1}{\beta} \cdot \frac{1}{|0.29 - 0.71j|} \approx \frac{1.3}{\beta}$

The frequency response of the feedback system suffers from a 30% peak at  $\omega = \omega_1$ .

- Close-loop frequency response for  $45^\circ$  phase margin:

