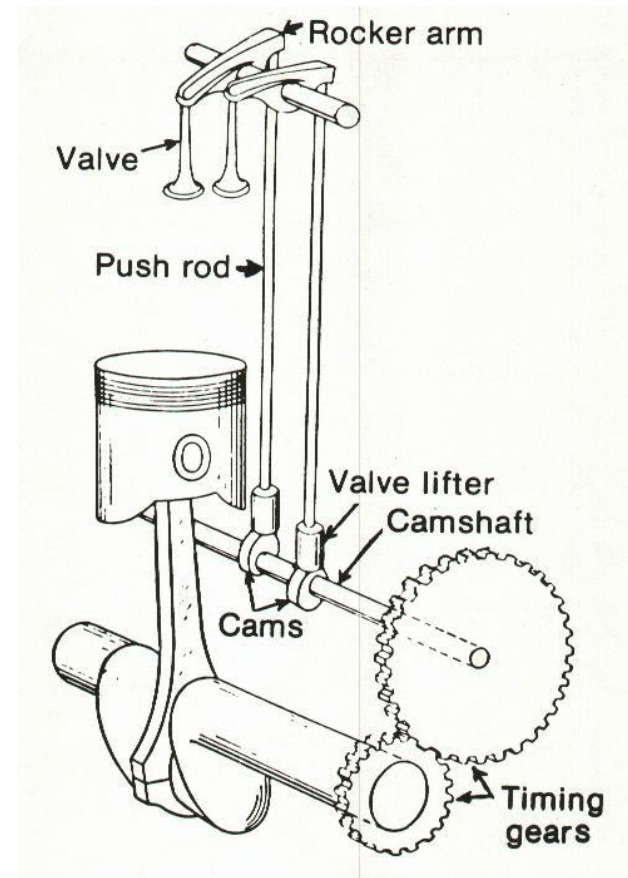


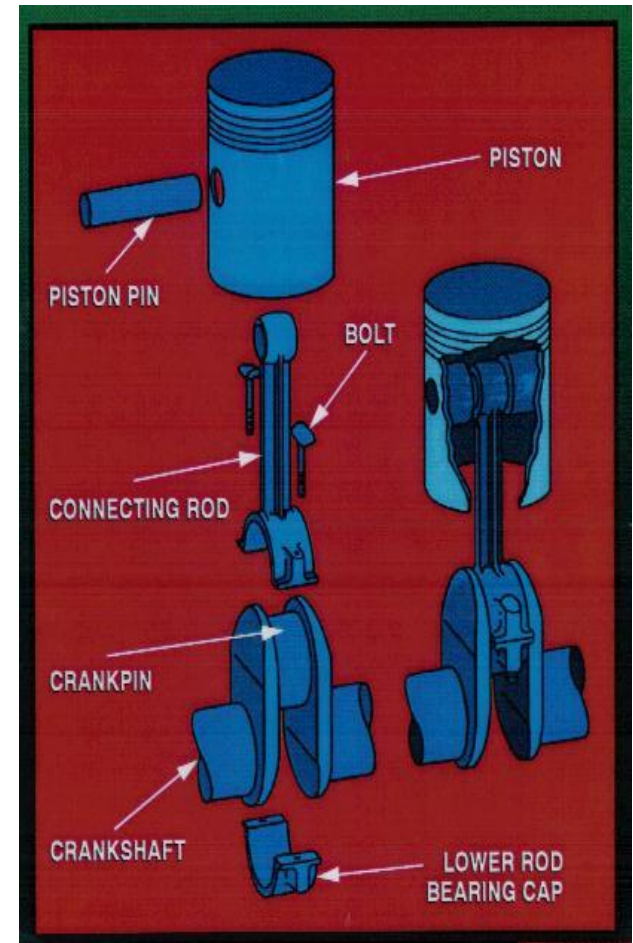
Moving Components of I C Engine

- Valves
 - Intake: open to admit air to cylinder (with fuel in Otto cycle)
 - Exhaust: open to allow gases to be rejected
- Camshaft & Cams
 - Used to time the addition of intake and exhaust valves
 - Operates valves via pushrods & rocker arms



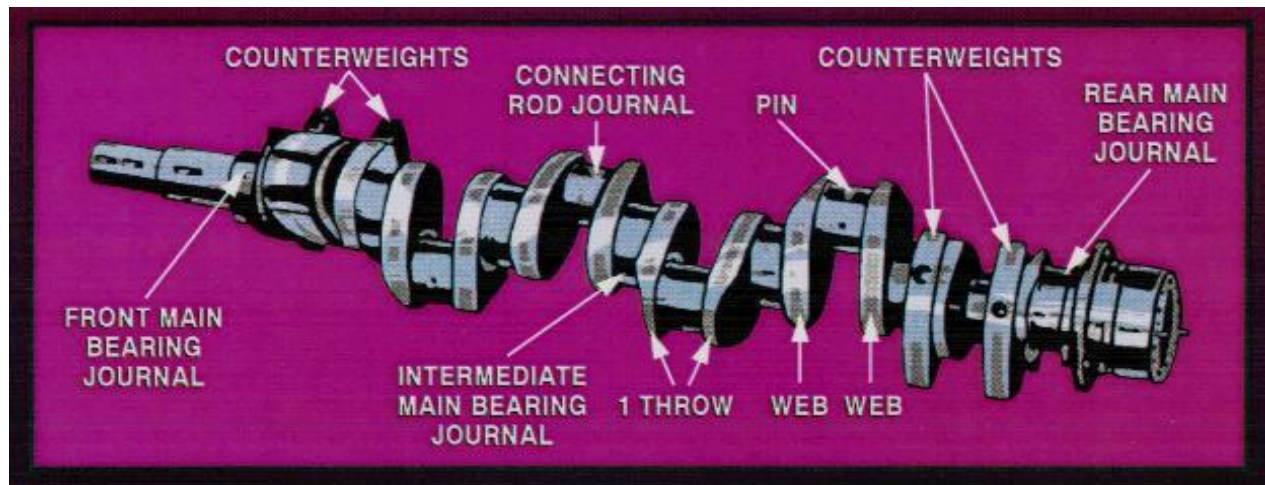
Moving Components

- Piston
 - Acted on by combustion gases
 - Lightweight but strong/durable
- Piston Rings
 - Transfer heat from piston to cylinder
 - Seal cylinder & distribute lube oil
- Piston Pin
 - Pivot point connecting piston to connecting rod
- Connecting Rod
 - Connects piston & crankshaft
 - reciprocating → rotating motion

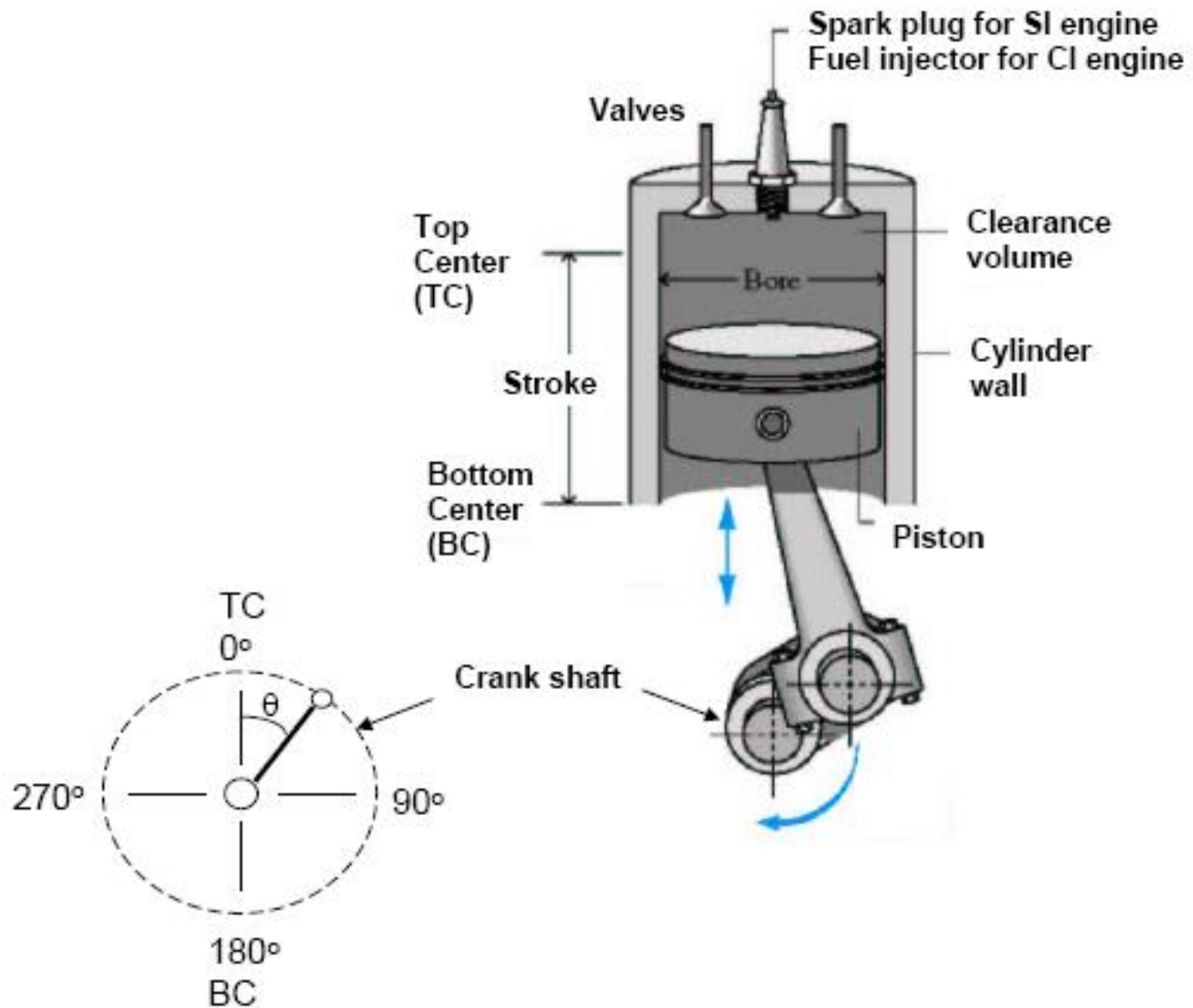


Moving Components

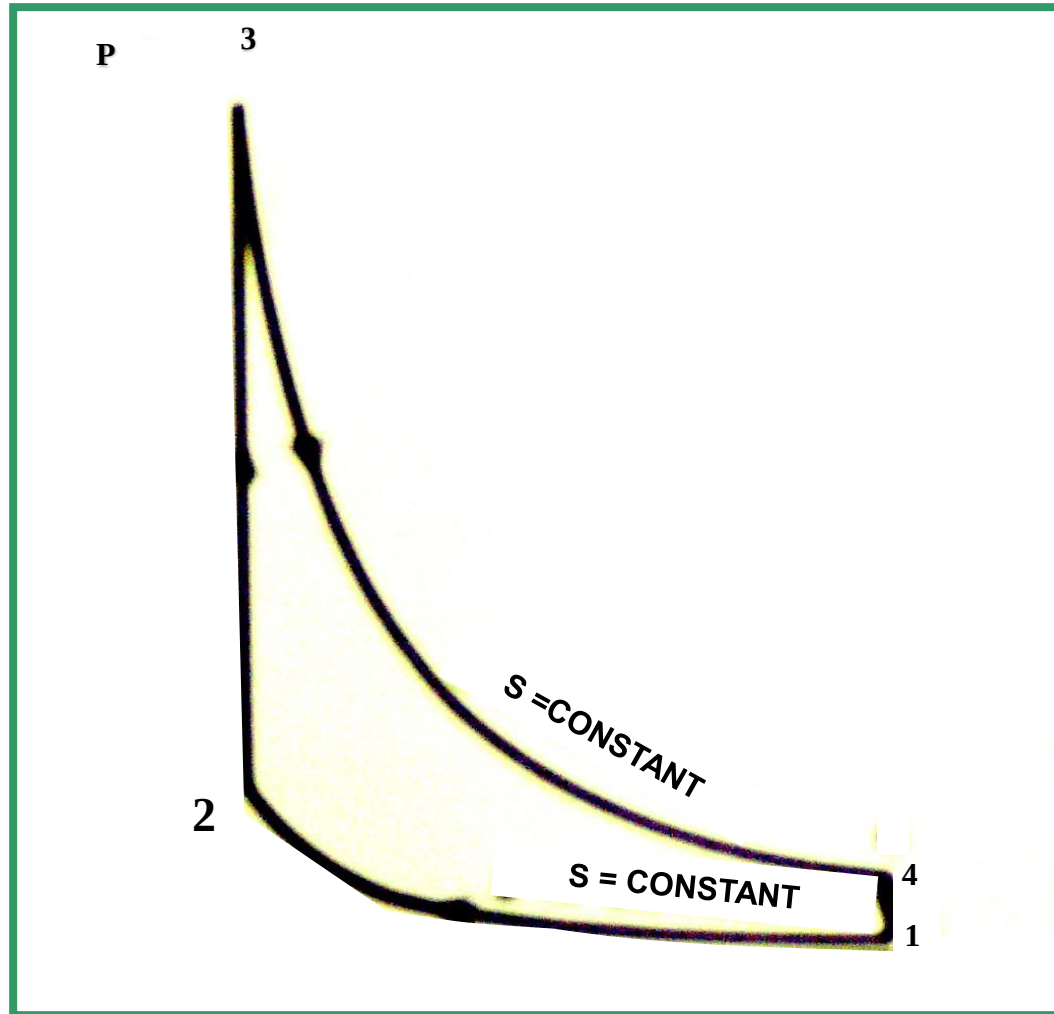
- Crankshaft
 - Combines work done by each piston
 - Drives camshafts, generator, pumps, etc.
- Flywheel
 - Absorbs and releases kinetic energy of piston strokes -> smoothes rotation of crankshaft



Otto (SI Engine) Operating Cycle



Air Standard Cycles



Otto Cycle: An ideal cycle that approximates a spark-ignition internal-combustion engine.

- Process:**
- 1-2 Isentropic Compression of Air**
 - 2-3 Heat Addition at Constant Volume**
 - 3-4 Isentropic Expansion**
 - 4-1 Rejection of Heat from the Working Fluid at Constant Volume**

Compression Ratio = $r_v = \frac{V_1}{V_2} = \frac{V_4}{V_3}$

Assuming constant specific heats of air:

$$\eta_{th} = \frac{Q_H - Q_L}{Q_H} = 1 - \frac{Q_L}{Q_H}$$

$$= 1 - \frac{mC_v(T_4 - T_1)}{mC_v(T_3 - T_2)}$$

$$= 1 - \frac{T_1(T_4 / T_1 - 1)}{T_2(T_3 / T_2 - 1)}$$

Since $\frac{V_1}{V_2} = \frac{V_4}{V_3}$, **processes are isentropic (1-2 and 3-4)**

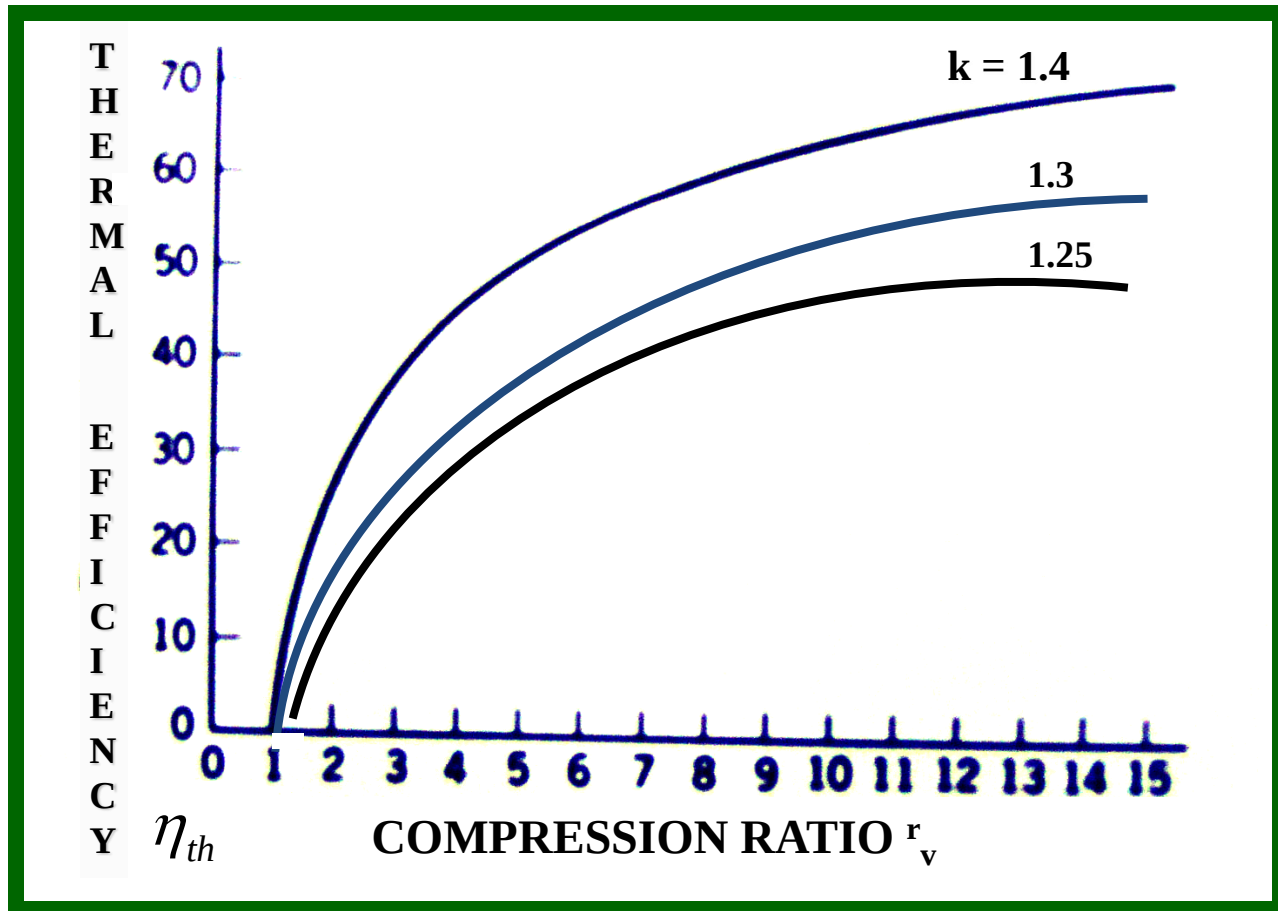
$$\therefore \frac{T_2}{T_1} = \left(\frac{V_1}{V_2} \right)^{k-1} = \left(\frac{V_4}{V_3} \right)^{k-1} = \frac{T_3}{T_4}$$

$$\frac{T_3}{T_2} = \frac{T_4}{T_1}$$

$$\eta_{th} = 1 - \frac{T_1}{T_2} = 1 - r_v^{(1-\kappa)} = 1 - \frac{1}{r_v^{\kappa-1}}$$

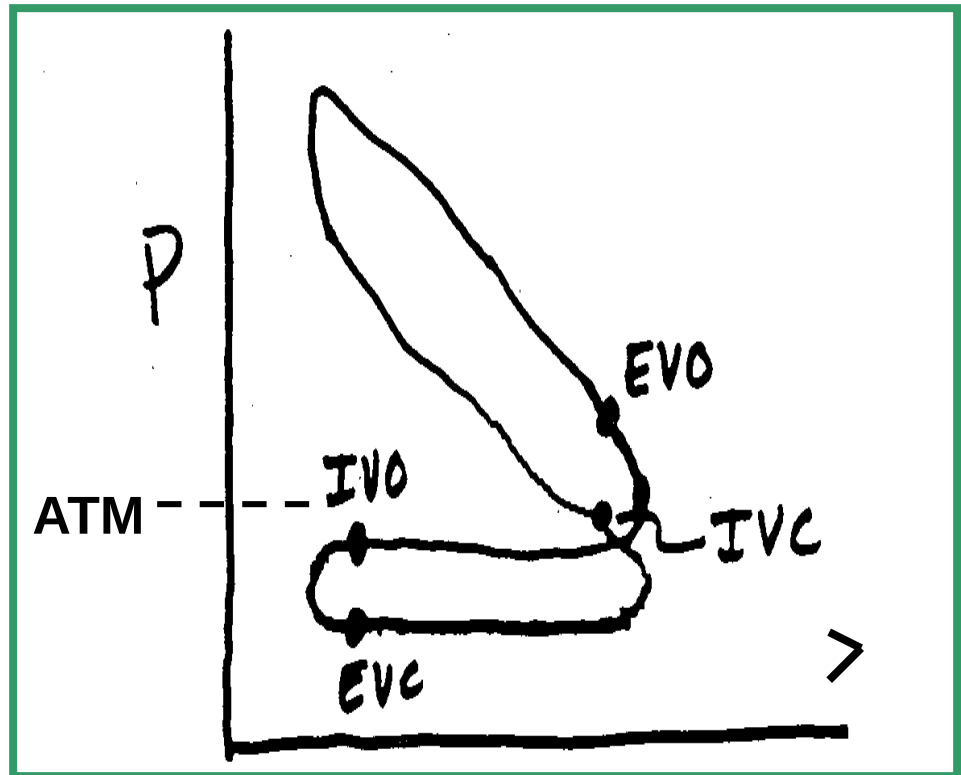
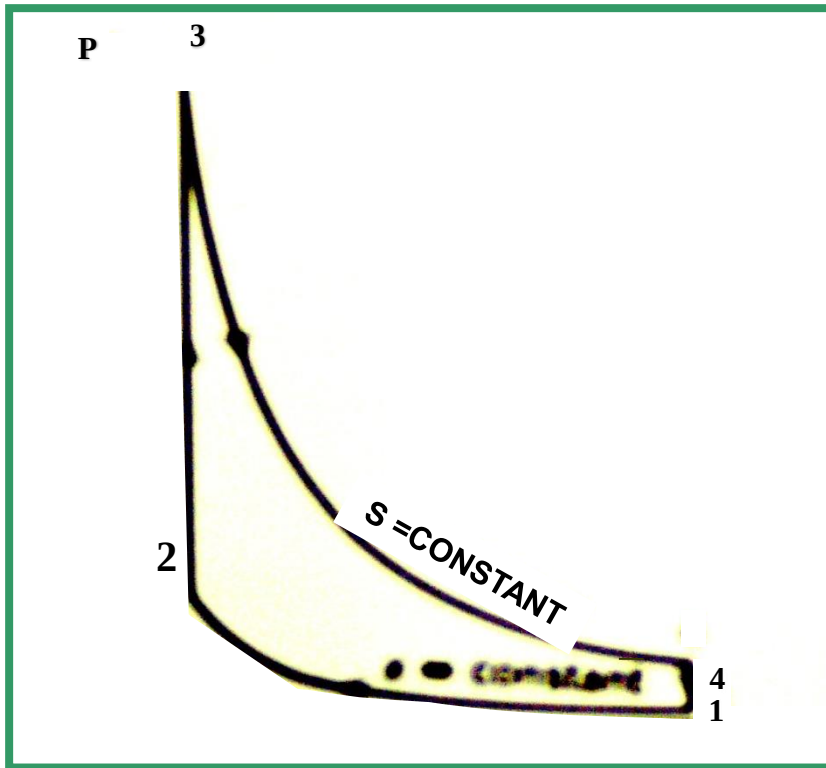
Note: Air standard Otto cycle is only a function of compression ratio.

Thermal Efficiency of the Otto Cycle as a Function of Compression Ratio



Thermal efficiency of an air-standard Otto Cycle as a function of compression ratio.

Comparison of air-standard cycle with an actual cycle



Primary Physical Differences

Air Standard Cycle vs. Actual Cycle

(Actual Cycle is Typical S-I 4-Stroke)

Process	Air Standard	Actual Cycle
1-2	Isentropic Compression of Air	Some heat-transfer, but in a good engine, peak pressure during motoring is nearly equal to the pressure calculated with isentropic relationships. Intake valve closes.
2-3	Constant Volume Heat Addition	Heat addition takes place over an interval of time. Heat is lost to piston, cylinder walls and to cylinder head during this time.
3-4	Isentropic Expansion Combustion is Complete	Combustion continues into the expansion stroke. Heat transfer takes place and energy is lost to cylinder walls, head and piston. Piston ring blow-by occurs, as well as blowback. Exhaust valve opens and a blowdown process begins.
4-1	Reject of Heat from Working Fluid While Piston is at Rest	Piston completes a mechanical stroke to expel spent exhaust gases and an intake stroke to induct fresh charges – pumping work occurs. Wave dynamics from other cylinders may be present.

Gas Laws

With constant pressure $\frac{V_1}{V_2} = \frac{T_1}{T_2}$

With constant volume $\frac{P_1}{P_2} = \frac{T_1}{T_2}$

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \dots = \frac{PV}{T} = R$$

$$PV = MRT$$

M = the mass of gas considered

P = the absolute pressure

V = the volume of the mass M

T = the absolute temperature

$$R = 8.314 \frac{\text{J}}{\text{g mole K}}$$

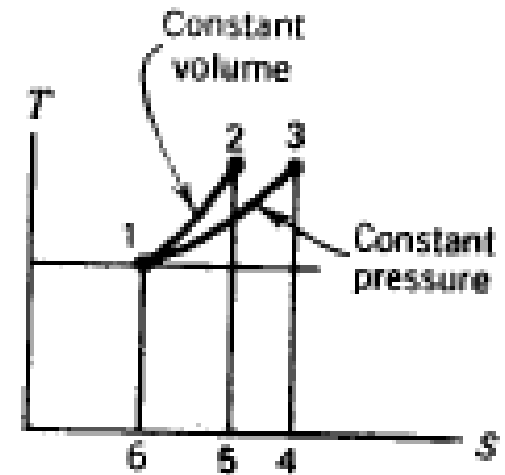
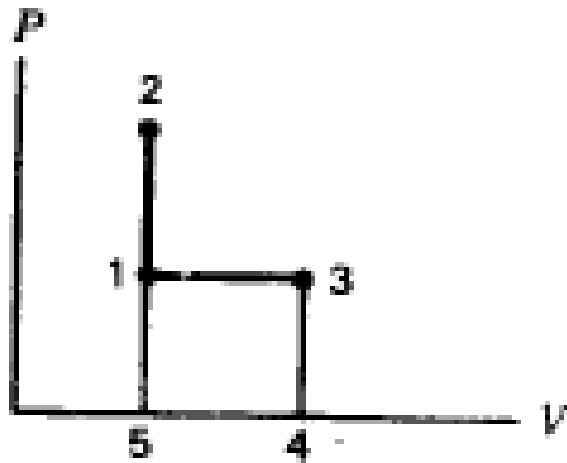
$$Q = Mc(T_2 - T_1) = (U_2 - U_1) + W$$

where Q = heat gained or rejected
 M = mass of the gas
 c = specific heat
 $(U_2 - U_1)$ = change in internal energy
 W = work done

c_v = specific heat at constant volume

c_p = specific heat at constant pressure

$k = c_p/c_v$



Constant Volume Changes

General Equation is

$$C_v (T_2 - T_1) = U_2 - U_1$$

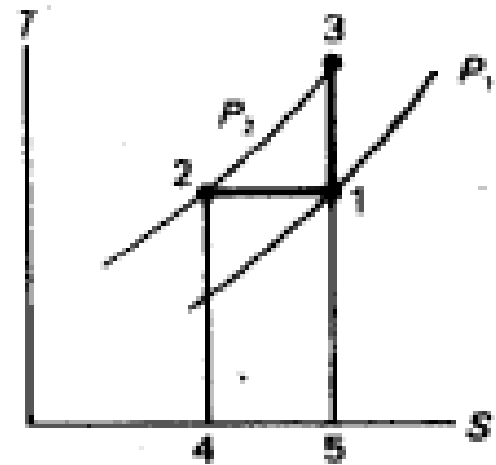
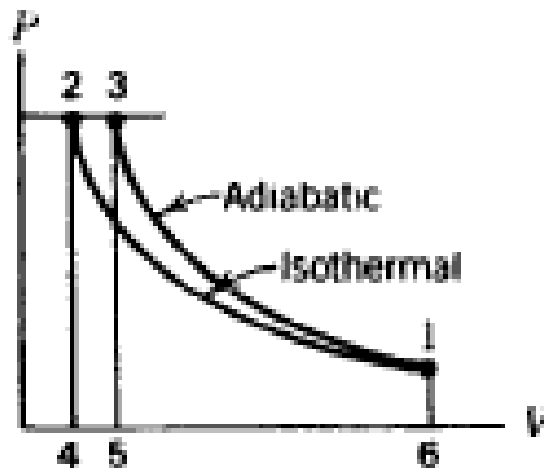
Constant Pressure Changes

$$C_p(T_3 - T_1) = C_v (T_3 - T_1) + P (V_3 - V_1),$$

But, $P_3V_3 = RT_3$, $P_1V_1 = RT_1$ and $P_1 = P_3$

$$\text{So, } C_p(T_3 - T_1) = C_v (T_3 - T_1) + R(T_3 - T_1)$$

$$\text{Or, } C_p - C_v = R$$



Isothermal Changes

$$PV = C \text{ (Constant) },$$

Boyles' Law

The work done during any change in volume from V_1 to V_2 is

$$W = \int_{V_1}^{V_2} P \, dV$$

$$W = \int_{V_1}^{V_2} \frac{C}{V} dV = C \int_{V_1}^{V_2} \frac{dV}{V} = C[\log_e V] \Big|_{V_1}^{V_2}$$

$$W = C(\log_e V_2 - \log_e V_1)$$

Since the initial conditions are $PV = C = P_1V_1$, this value may be substituted in equation 16 to obtain

$$W = P_1V_1(\log_e V_2 - \log_e V_1)$$

or

$$W = P_1V_1 \log_e \frac{V_2}{V_1}$$

For any mass of gas other than unity there may be substituted

$$P_1V_1 = MRT$$

and

$$\frac{V_2}{V_1} = \frac{P_1}{P_2}$$

The work is

$$W = MRT \log_e \frac{V_2}{V_1} = MRT \log_e \frac{P_1}{P_2}$$

Letting $r = V_1/V_2$ be the compression ratio or ratio of expansion, we have

$$W = MRT \log_e \frac{1}{r}$$

Adiabatic or constant Entropy Changes

$$0 = c_v(T_3 - T_1) + W$$

$$W = -c_v(T_3 - T_1)$$

unit mass

$$W = -c_v \left(\frac{P_3 V_3}{R} - \frac{P_1 V_1}{R} \right) = -\frac{1}{R} c_v (P_3 V_3 - P_1 V_1)$$

$$R = c_p - c_v$$

$$W = -\frac{c_v}{c_p - c_v} (P_3 V_3 - P_1 V_1)$$

$$W = \frac{P_3 V_3 - P_1 V_1}{1 - k} = \frac{P_1 V_1 - P_3 V_3}{k - 1}$$

unit mass of gas.

For M mass units of gas,

$$W = \frac{MR(T_1 - T_3)}{k - 1}$$

General or Polytropic Changes

$$W = \int P dV$$
$$P_1 V_1^n = P V^n$$

$$P = P_1 V_1^n \frac{1}{V^n}$$

Substituting,

$$\begin{aligned} W &= P_1 V_1^n \int_{V_1}^{V_2} \frac{dV}{V^n} = P_1 V_1^n \int_{V_1}^{V_2} V^{-n} dV \\ &= \frac{P_1 V_1^n}{1-n} (V_2^{1-n} - V_1^{1-n}) \\ &= \frac{P_1 V_1^n V_2^{1-n} - P_1 V_1^n V_1^{1-n}}{1-n} \end{aligned}$$

Substituting $P_1 V_1^n = P_2 V_2^n$,

$$W = \frac{P_2 V_2^n V_2^{1-n} - P_1 V_1^n V_1^{1-n}}{1-n} = \frac{P_2 V_2 - P_1 V_1}{1-n}$$

If $n = k$, then

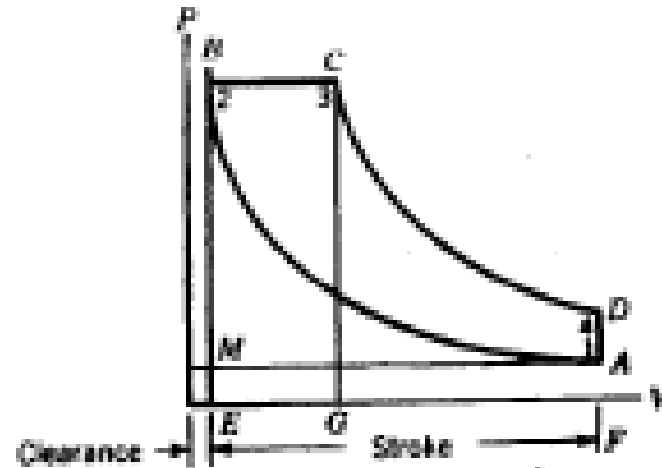
$$W = \frac{P_2 V_2 - P_1 V_1}{1-k}$$

$$\begin{aligned}
 T_2 &= T_1 \left(\frac{V_2}{V_1} \right)^{1-\gamma} = T_1 \left(\frac{V_1}{V_2} \right)^{\gamma-1} = T_1 \left(\frac{P_2}{P_1} \right)^{(\gamma-1)/\gamma} \\
 &= T_1 \left(\frac{P_2}{P_1} \right)^{1-(1/\gamma)}
 \end{aligned}$$

$$P_2 = P_1 \left(\frac{V_1}{V_2} \right)^{\gamma} = P_1 \left(\frac{T_2}{T_1} \right)^{\gamma/(\gamma-1)}$$

$$V_2 = V_1 \left(\frac{P_1}{P_2} \right)^{1/\gamma} = V_1 \left(\frac{T_1}{T_2} \right)^{1/(\gamma-1)}$$

EFFICIENCY OF DIESEL CYCLE



$$Q_{in} = Mc_p(T_3 - T_2) \qquad Q_{out} = Mc_v(T_4 - T_1)$$

$$\begin{aligned} e &= \frac{Q_{in} - Q_{out}}{Q_{in}} = 1 - \frac{Q_{out}}{Q_{in}} \\ &= 1 - \frac{Mc_v(T_4 - T_1)}{Mc_p(T_3 - T_2)} = 1 - \frac{(T_4 - T_1)}{k(T_3 - T_2)} \\ &= 1 - \frac{T_1}{T_2} \left[\frac{\left(\frac{T_4}{T_1} - 1\right)}{k\left(\frac{T_3}{T_2} - 1\right)} \right] \end{aligned}$$

$$T_3 = T_2 \frac{V_3}{V_2} \text{ at constant pressure}$$

$$T_4 = T_3 \left(\frac{V_3}{V_4} \right)^{\gamma-1} \text{ adiabatically}$$

$$T_4 = T_2 \frac{V_3}{V_2} \left(\frac{V_3}{V_4} \right)^{\gamma-1} = T_2 \frac{(V_3/V_2)^{\gamma}}{(V_4/V_2)^{\gamma-1}}$$

Since the compression from 1 to 2 is adiabatic and $V_4 = V_1$, we have

$$T_2 = T_1 \left(\frac{V_4}{V_2} \right)^{\gamma-1}$$

Solving for T_1 and then dividing T_4 by T_1 we obtain

$$\frac{T_4}{T_1} = \frac{(V_4/V_2)^{\gamma-1}(V_3/V_2)^{\gamma}}{(V_4/V_2)^{\gamma-1}} = \left(\frac{V_3}{V_2} \right)^{\gamma}$$

$$e = 1 - \frac{T_1[(V_3/V_2)^k - 1]}{kT_2[(V_3/V_2) - 1]}$$

$$T_1 = T_2 \left(\frac{V_2}{V_1} \right)^{k-1}$$

$$e = 1 - \left\{ \frac{(V_2/V_1)^{k-1} [(V_3/V_2)^k - 1]}{k[(V_3/V_2) - 1]} \right\}$$

$$= 1 - \frac{1}{(V_1/V_2)^{k-1}} \left[\frac{(V_3/V_2)^k - 1}{k[(V_3/V_2) - 1]} \right]$$

$$e = 1 - \frac{1}{r^{k-1}} \left[\frac{(V_3/V_2)^k - 1}{k[(V_3/V_2) - 1]} \right]$$

